

時事問題解析工房出版物の訂正補足通知。

過去出版物リスト(著者=鈴木基司) : 2017/4/21

(1)量子確率過程力学、時事問題解析工房、初版1990→最終版1996
(2)(上記英文版在り)

(3)非局所的な双極子場の量子論<改定中>、時事問題解析工房、1992.

(4)構造的物理認識の為の連続値論理学、時事問題解析工房、1992→1996.

(5)量子重力力学と最終統一場論、時事問題解析工房、1993→1997.

*上記量子物理学全般+数学等の要綱公式集私用マニュアル file 本在り、

(6)思考推進言語と真相世界、時事問題解析工房、1993→1997.

(7)現代物理科学最前線、時事問題解析工房、1998→1999.

(8)経済回路網力学、時事問題解析工房、1998.

(9)縦波電位波発電の理論と実現、時事問題解析工房、2003.

(10)新量子物理学の一般紹介本(1995) → 原稿盗難 (ファイル4冊)、
高校上級, 大学教養程度の基礎数学&物理を前提、

* アナログ録音機ワ-プロ保存データ在り、だがワ-プロ修理不能で放置状態、
マシン=サンヨ-SWP M12

*通うなデータを復元, ワード形式変換の商売が存在, だが費用高価です.

*原稿文のスキヤナ読み取りでワード形式変換の可能性?

(11)日本の癌病巣をえぐる(I , II , III)

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出版物の訂正補足通知。

2017/4/21.

(1)量子確率過程力学(1996). →p76.

$$|\Upsilon(\Delta u; t)| = [1 - (\Delta u \Delta \varepsilon / \hbar)^2]^{1/2}. \quad (6-3-21)$$

誤箇所: $\sqrt{(1-x^2)} = 1-x$. → 詳細訂正内容は次3ページ、本筋結論は不変です。

(5)量子重力力学と最終統一場論(1997). →p23.

誤箇所: $R^Q = \Pi_{a, \mu, \nu, x} \int D A_\mu^a \int D \Pi_\nu^a \int D B^a \int D f^a \cdot \Delta \cdot \delta(ic \partial_\mu A_\mu^a - f^a)$
 $\exp[\int dx^4 \langle \mathcal{L}_{CF} / i\hbar \rangle] \cdot \exp[\int dx^4 (B^a f^a + 1/2 a B^a B^a) / i\hbar]$

→ 訂正内容

$$R^Q = \Pi_{a, \mu, \nu, x} \int D \varepsilon^3 \cdot \int D A_\mu^a \int D \Pi_\nu^a \int D B^a \int D \bar{C}^a \int D C^a \cdot \exp[\int dx^4 \langle \mathcal{L}_{CF} / i\hbar \rangle] \cdot$$
$$\delta(ic \partial_\mu A_\mu^a - f^a) \cdot \exp[\int dx^4 (B^a f^a + 1/2 a B^a B^a) / i\hbar] \cdot \exp[\int dx^4 \cdot \chi \bar{C}^a(x) \cdot ic \partial_\mu D_\mu C^a(x) / i\hbar]$$

→ 詳細補足訂正内容は次ページ、本筋結論は不変です。

**[2] : Time & Energy Uncertainty Relation by the Statistical Mathematics :
 “Evolution Principle by Energy Fluctuation”.**

Time domain **Corelation Function** is measure for function shape similarity intensity of $\Psi(t)$ and $\Psi(t+\Delta t)$, while the frequency domain representation give us deep insight on **time and energy uncertainty principle in state decaying**. This is not dynamics, but mere a math principle.

① semi macroscopic finite integral time duration: $T(t) \equiv [t - \Delta T/2, t + \Delta T/2]$.

② Fourier component of $\Psi(t)$: $c(\epsilon; t) \equiv (2\pi\hbar)^{-1/2} \int_{T(t)} du |\Psi(t)\rangle \exp(\epsilon u / i\hbar)$

③ **State density**: $\omega(\epsilon; t) \equiv \langle c(\epsilon; t) | c(\epsilon; t) \rangle / \Delta T$
 $= (\Delta T \cdot 2\pi\hbar)^{-1} \int_{T(t)} du \int_{T(t)} dv \langle \Psi(u) | \Psi(v) \rangle \exp(-\epsilon(u-v)/i\hbar)$.

④ **Inverse Transform**: $\int_{-\infty}^{\infty} d\epsilon \exp(-\epsilon \Delta u / i\hbar) \omega(\epsilon; t)$
 $= (\Delta T \cdot 2\pi\hbar)^{-1} \int_{T(t)} du \int_{T(t)} dv \langle \Psi(u) | \Psi(v) \rangle \int_{-\infty}^{\infty} d\epsilon \exp(-\epsilon(\Delta u + u - v) / i\hbar)$
 $= (\Delta T)^{-1} \int_{T(t)} du \int_{T(t)} dv \langle \Psi(u) | \Psi(v) \rangle \delta(\Delta u + u - v) = (\Delta T)^{-1} \int_{T(t)} du \langle \Psi(u) | \Psi(\Delta u + u) \rangle$

⑤ **modified Winer Kinchin Thorem for non Equilibrium Statistical Mechanics.**
 $(\Delta T)^{-1} \int_{T(t)} du \langle \Psi(u) | \Psi(\Delta u + u) \rangle \equiv \Upsilon(\Delta u; t) = \int_{-\infty}^{\infty} d\epsilon \exp(-\epsilon \Delta u / i\hbar) \omega(\epsilon; t)$
 $= \int_{-\infty}^{\infty} d\epsilon \omega(\epsilon; t) [1 - i\epsilon \Delta u / \hbar - \epsilon^2 \Delta u^2 / \hbar^2 / 2 + \dots] = 1 + i\langle \epsilon \rangle \Delta u / \hbar - \langle \epsilon^2 \rangle (\Delta u / \hbar)^2 / 2 + \dots$

⑥ $|\Upsilon(\Delta u; t)| = [(1 - \langle \epsilon^2 \rangle (\Delta u / \hbar)^2 / 2) + \langle \epsilon^2 \rangle \Delta u^2 / \hbar^2]^{1/2} + \dots$
 $= [1 - \langle \epsilon^2 \rangle (\Delta u / \hbar)^2 + \langle \epsilon^2 \rangle \Delta u^2 / \hbar^2 + \langle \epsilon^2 \rangle^2 (\Delta u / \hbar)^4 / 4]^{1/2} + \dots$
 $= [1 - (\Delta u / \hbar)^2 [\langle \epsilon^2 \rangle - \langle \epsilon \rangle^2] + \dots]^{1/2} = [1 - (\Delta u \Delta \epsilon / \hbar)^2]^{1/2} + \dots$

⑦ $1 \geq |\Upsilon(\Delta t; t)| \geq 0$ and the meaning of Energy and Time uncertainty principle.
 | Υ | **the corelation function** is measure for **state decaying rate** by time = Δt for initial state = $\Psi(t)$ to final state = $\Psi(\Delta t + t)$. If $\Delta t \Delta \epsilon = \hbar$, then $|\Upsilon(\Delta t; t)| = 0$, which means **transition completion** from initial state = $\Psi(t)$ to final state = $\Psi(t + \Delta t)$.

[2]: ⑦ Energy and Time Uncertainty Principle.
“Evolution Principle by Energy Fluctuation”.
 $\Delta t \Delta E = \hbar$.
 ΔE = **energy deviation** in statistical ensemble.
 Δt = **transition time** in statistical ensemble by ΔE .

APPENDIX3:Deriving FP Lagrangean by Path-Integral. 2017/4/10

Gauge Covariant Quantized Lagrangean must be with $0=i_c \partial_\mu D_\mu \epsilon^a$, which is kernel. Feynman Path Integral, Variable transform and Jacobian in integral calculation are tools. Consequently, we derive Faddeev-Popov Lagrangean term in **Gauge Field Quantization**.

*This is alternative of [5] : **Quantized Lagrangean of $\{\bar{C}^a, C^a\}$ <FP Gohst>**.

*L.D.Faddeev and V.N.Popov:Pphys Lett.25B(1967)29.

“Feynman Diagram for The Yang-Mills Field”

Feynman, R. P. (1948). *Reviews of Modern Physics*. **20 (2): 367–387.

"Space-Time Approach to Non-Relativistic Quantum Mechanics".

[1] : Schrödinger EQN Solution by Path-Integral.

$$(1) i\hbar \partial_t \Psi(t) = H(t) \Psi(t). \rightarrow \Psi(t+\Delta t) = [1 + \Delta t/i\hbar H(t)] \Psi(t)$$

Difficulty of time & energy variable by uncertainty principle(UP) in Quantum Mechanics.

H(t) is energy observable, while (t) is time, which are ruled by UP ($\Delta E \Delta t = \hbar$). Thereby, both can not be determined simultaneously without 0 error. Discussion at here is to **neglect the fact(classical calculation)**, so it is inevitable to face **some difficulty** to derive definite result.

<http://www.777true.net/img007-Quick-Guide-to-Quantum-Stochastic-Mechanics.pdf>

☞ : time at here is mere events sequence parameters $t_j > t_{j-1}$, but not time value.

$$(2) \Psi(t_0+n \Delta t=t) = [1 + (\Delta t/i\hbar) H(t_0+\langle n-1 \rangle \Delta t)] \Psi(t_0+\langle n-1 \rangle \Delta t)$$

$$\Psi(t_0+\langle n-1 \rangle \Delta t) = [1 + (\Delta t/i\hbar) H(t_0+\langle n-2 \rangle \Delta t)] \Psi(t_0+\langle n-2 \rangle \Delta t)$$

$$\dots \Psi(t_0+\Delta t) = [1 + (\Delta t/i\hbar) H(t_0+0 \Delta t)] \Psi(t_0+0 \Delta t=t_0).$$

$$\Psi(t) =_{n \rightarrow \infty} [1 + (\Delta t/i\hbar) H(t_{n-1})] \times [1 + (\Delta t/i\hbar) H(t_{n-2})] \times \dots \times [1 + (\Delta t/i\hbar) H(t_j)] \times [1 + (\Delta t/i\hbar) H(t_1)] \times [1 + (\Delta t/i\hbar) H(t_0)] \Psi(t_0) \equiv S(t; t_0) \Psi(t_0)$$

$R_{fi} \equiv \langle \Psi(t) | S(t; t_0) | \Psi(t_0) \rangle \equiv$ transition probability amplitude from $\Psi(t_0) \rightarrow \Psi(t)$.

(3)Representation by (Q ; P) Space and Momentum Observable's Eigen Function Set.

- (a) $P |p\rangle = -i\hbar \partial_q | \exp(-pq/i\hbar) \rangle / \sqrt{2\pi\hbar}$.
- $\langle p' | p \rangle = \int_{-\infty}^{\infty} dq \exp(p'q/i\hbar) \exp(-pq/i\hbar) / (2\pi\hbar) = \delta(p-p')$.
- (b) $Q |q\rangle = q' \delta(q-q')$.
- (c) $\langle q | p \rangle \equiv \int dq' \delta(q-q') \exp(-pq'/i\hbar) \rangle / \sqrt{2\pi\hbar} \equiv \exp(-pq/i\hbar) \rangle / \sqrt{2\pi\hbar}$.
- $\langle p | q \rangle \equiv \int_{-\infty}^{\infty} dq' \delta(q-q') \exp(pq'/i\hbar) \rangle / \sqrt{2\pi\hbar} \equiv \exp(pq/i\hbar) \rangle / \sqrt{2\pi\hbar}$.
- (d) **unit operator 1** $\equiv \int dq |q\rangle \langle q| = \int dq |p\rangle \langle p|$;

(4) **QP representation of $S(t; t_0)$.**

$$\begin{aligned}
 S(t; t_0) &= \int dq_{n-1} |q_{n-1}\rangle \langle q_{n-1}| [1 + (\Delta t / i\hbar) \mathbf{H}(t_{n-1})] \int dp_{n-1} |p_{n-1}\rangle \langle p_{n-1}| \\
 &\times \int dq_{n-2} |q_{n-2}\rangle \langle q_{n-2}| [1 + (\Delta t / i\hbar) \mathbf{H}(t_{n-2})] \int dp_{n-2} |p_{n-2}\rangle \langle p_{n-2}| \times \\
 &\dots \\
 &\times \int dq_j |q_j\rangle \langle q_j| [1 + (\Delta t / i\hbar) \mathbf{H}(t_j)] \int dp_j |p_j\rangle \langle p_j| \times \\
 &\dots \\
 &\times \int dq_1 |q_1\rangle \langle q_1| [1 + (\Delta t / i\hbar) \mathbf{H}(t_1)] \int dp_1 |p_1\rangle \langle p_1| \\
 &\times \int dq_0 |q_0\rangle \langle q_0| [1 + (\Delta t / i\hbar) \mathbf{H}(t_0)] \int dp_0 |p_0\rangle \langle p_0| \\
 &\times \int dq_{-1} |q_{-1}\rangle \langle q_{-1}|
 \end{aligned}$$

$$\begin{aligned}
 S(t; t_0) &= \prod_{j=-1}^{n-1} \int dq_j \prod_{j=0}^{n-1} \int dp_j |q_{n-1}\rangle \langle q_{-1}| \\
 &\times \{ \prod_{j=0}^{n-1} \langle q_j | [1 + (\Delta t / i\hbar) \mathbf{H}(t_j)] |p_j\rangle \langle p_j | q_{j-1}\rangle \}
 \end{aligned}$$

$$\begin{aligned}
 * \langle q_j | [1 + \Delta t / i\hbar] \mathbf{H}(t_j) |p_j\rangle \langle p_j | q_{j-1}\rangle &= [\langle q_j | p_j\rangle + \Delta t / i\hbar \langle q_j | \mathbf{H}(t_j) |p_j\rangle] \langle p_j | q_{j-1}\rangle \\
 &= [\exp(-q_j p_j / i\hbar) / \sqrt{2\pi\hbar} + (\Delta t / i\hbar) \langle q_j | \mathbf{H}(t_j) |p_j\rangle] \exp(p_j q_{j-1} / i\hbar) / \sqrt{2\pi\hbar} \\
 &= \exp(-p_j \langle q_j - q_{j-1}\rangle / i\hbar) / (2\pi\hbar) + (\Delta t / i\hbar) \langle q_j | \mathbf{H}(t_j) |p_j\rangle \exp(p_j q_{j-1} / i\hbar) / \sqrt{2\pi\hbar} \\
 &= \exp(-p_j \langle q_j - q_{j-1}\rangle / i\hbar) / (2\pi\hbar) [1 + (\Delta t / i\hbar) \langle q_j | \mathbf{H}(t_j) |p_j\rangle \exp(p_j q_{j-1} / i\hbar) \sqrt{2\pi\hbar}]
 \end{aligned}$$

* **useful formula: $1 + \delta X = \exp(\delta X)$**

$$\begin{aligned}
 * \exp(-p_j \langle q_j - q_{j-1}\rangle / i\hbar) &= \exp(-\Delta t \cdot p_j (dq_j / dt) / i\hbar). \\
 ** |p_j'\rangle &= \exp(-p_j' q_j / i\hbar) / \sqrt{2\pi\hbar}. \rightarrow \langle p' | p\rangle = \delta(p - p'). \\
 \langle q_j | \mathbf{H}(t_j) |p_j\rangle \sqrt{2\pi\hbar} \exp(p_j q_j / i\hbar) &= \int dq_j' \mathbf{H}(q_j; p_j) \delta(q_j - q_j') \exp(p_j q_j / i\hbar) \exp(-p_j q_j' / i\hbar) \\
 &= \mathbf{H}(q_j; p_j).
 \end{aligned}$$

$$\begin{aligned}
 &= (2\pi\hbar)^{-1} \cdot \exp[-(\Delta t / i\hbar) \cdot p_j (dq_j / dt)] \exp[(\Delta t / i\hbar) \cdot \mathbf{H}(q_j; p_j)] \\
 &= (2\pi\hbar)^{-1} \cdot \exp[-(\Delta t / i\hbar) \langle \mathcal{L}(q_j; dq_j / dt) \rangle]. \quad \langle \text{useful formula: } 1 + \delta X = \exp(\delta X) \rangle
 \end{aligned}$$

$$\begin{aligned}
 S(t; t_0) &= \prod_{j=-1}^{n-1} \int dq_j \prod_{j=0}^{n-1} \int dp_j |q_{n-1}\rangle \langle q_{-1}| \\
 &\times \{ \prod_{j=0}^{n-1} (2\pi\hbar)^{-n} \cdot \exp[-(\Delta t / i\hbar) \langle \mathcal{L}(q_j; dq_j / dt) \rangle] \}. \\
 &= \prod_{j=-1}^{n-1} \int dq_j \prod_{j=0}^{n-1} \int (dp_j / 2\pi\hbar) \cdot |q_{n-1}\rangle \langle q_{-1}| \cdot \exp[-\int dt \langle \mathcal{L}(q_j; dq_j / dt) / i\hbar \rangle] \\
 &\equiv |f\rangle \langle i| \int Dq_j \int Dp_j \cdot \exp[-\int dt \langle \mathcal{L}(q; dq / dt) / i\hbar \rangle] \dots \text{this is the origin definition !!}
 \end{aligned}$$

(4) **Quantum Amplitude = R_{fi} by Feymann Path Integral .**

$$\begin{aligned}
 \mathbf{S}(t; t_0) &= |f\rangle \langle i| \int_{-\infty}^{\infty} Dq \int_{-\infty}^{\infty} Dp \cdot \exp[-\int_{t_0}^t dt \langle \mathcal{L}(q; dq / dt) / i\hbar \rangle]. \\
 R_{fii} &= \langle f | \mathbf{S}(t; t_0) | i \rangle.
 \end{aligned}$$

Operator part is $|f\rangle \langle i|$, the other are scalar term. This is not path-integral, but whole phase space one !.

[2] : Gauge Fixing by Path-Integral.

$$(1) \mathcal{L}_{CF} \equiv -\frac{1}{4} (\partial_\mu A^a_\nu - \partial_\nu A^a_\mu - f_{bc}^a A^b_\mu A^c_\nu)^2 \equiv -\frac{1}{4} F^a_{\mu\nu} F^a_{\mu\nu}.$$

$$\mathcal{L}_{GF} \equiv \mathcal{L}_{CF} + \mathcal{L}_B = (ic)^{-1} B^a \partial_\mu A^a_\mu + \frac{1}{2} \alpha B^a B^a.$$

$$(2) 0 = (ic)^{-1} \partial_\mu A^a_\mu + \alpha B^a.$$

The Euler Equation (2) must be gauge invariant by δA^a_μ .

$$(3) 0 = ic \partial_\mu A^a_\mu + \alpha B^a = ic \partial_\mu (A^a_\mu + \delta A^a_\mu) + \alpha B^a = ic \partial_\mu \delta A^a_\mu = ic \partial_\mu D_\mu \epsilon^a = 0 \dots \dots$$

$$(4) R_{CF} \equiv |f\rangle \langle i| \Pi_{a,\mu,x} \int D A^a_\mu \int D \Pi^a_\nu \cdot \exp[-\int dx^4 \langle \mathcal{L}_{CF}(A^a_\mu; \partial_\nu A^a_\mu) / i\hbar \rangle].$$

(5) **The Aim of Problem.**
 At first, note that gauge transform never change observable physics.
 In above, the integration $\int D A^a_\mu$ is to over-count due to gauge transform ∞ freedom, thereby **gauge fixing** by $\delta(ic \partial_\mu D_\mu \epsilon^a)$ must be multiply the integral kernel to R_{CF} . However the compensation = Δ is simultaneously necessary toward being unity. $\int d\epsilon \delta(k\epsilon) = 1/|k|$.
 (5) $1 = \Pi_{a,\mu,x} \int D \epsilon^a \cdot \Delta \cdot \delta(ic \partial_\mu D_\mu \epsilon^a)$.

(6) Review on **measure compensation = Jacobian** in integral variable transform.

<http://tutorial.math.lamar.edu/Classes/CalcIII/ChangeOfVariables.aspx>

$$\Rightarrow y^b = f^b(t^1, t^2, \dots, t_N) \Leftrightarrow t^a = g^a(y^b) = f^{a-1}(y^b). \quad \langle a, b=1, 2, 3, \dots, N \rangle$$

$$\Pi_a dt^a = \Pi_b dy^b \cdot \det | \partial g^a / \partial y^b | = \Pi_b dy^b \cdot \det | \partial f^a / \partial y^b |^{-1}.$$

$$\Pi_a \int dt^a \delta [f^1(t^1, t^2, \dots), f^2(\dots), \dots] = \Pi_b \int dy^b \delta (y^1, y^2, \dots) \det | \partial f^a / \partial y^b |^{-1} = \det | \partial f^a / \partial y^b |^{-1}.$$

$$\Rightarrow 1 = \Pi_a \int dt^a \delta (f^1(t^1, t^2, \dots), f^2(\dots), \dots) \det | \partial f^a / \partial y^b | \Rightarrow \Delta = \det | \partial f^a / \partial y^b | \dots (6)$$

(7) Deriving Δ .

$$(3) 0 = ic \partial_\mu A^a_\mu + \alpha B^a = ic \partial_\mu (A^a_\mu + \delta A^a_\mu) + \alpha B^a = ic \partial_\mu \delta A^a_\mu = ic \partial_\mu D_\mu \epsilon^a = 0 \dots \dots$$

$$ic \partial_\mu D_\mu \epsilon^a \equiv f^a \rightarrow \epsilon^a = (ic \partial_\mu D_\mu)^{-1} f^a.$$

$$\rightarrow \Pi_a D \epsilon^a = \Pi_b D f^b \cdot \det | \partial \{ (ic \partial_\mu D_\mu)^{-1} f^b \} / \partial f^b | = \Pi_b D f^b \cdot \det | (ic \partial_\mu D_\mu)^{-1} |.$$

$$\rightarrow \Pi_a D \epsilon^a = \Pi_b D f^b \cdot \det | (ic \partial_\mu D_\mu)^{-1} | \dots \dots \dots (7)'$$

$$\Rightarrow 1 = \Pi_{a,x} \int D \epsilon^a \cdot \delta (ic \partial_\mu D_\mu \epsilon^a) \cdot \det | (ic \partial_\mu D_\mu) | \Rightarrow \Delta = \det | ic \partial_\mu D_\mu | \dots (7)$$

Above relation is to be changed as follows. This is very important.

\Rightarrow Note we take **technic** $\langle (7)' \rangle$ in following doing integration on variables = $\{ \epsilon^a; f^a = f^a(\epsilon^a) \}$.

$$1 = \Pi_{a,x} \int D f^a \cdot \delta (-f^a) = \Pi_{a,x} \int D f^a \cdot \delta (ic \partial_\mu A^a_\mu - f^a)$$

$$= \Pi_{a,x} \int \Delta^{-1} D f^a \cdot \delta (ic \partial_\mu A^a_\mu - f^a) \cdot \Delta = \Pi_{a,x} \int D \epsilon^a \cdot \delta (ic \partial_\mu A^a_\mu - f^a) \cdot \Delta.$$

(8) Gauss Fresnel Integral Formula $\langle \int dx \cdot \exp(-ax^2/2) = \sqrt{(2\pi/a)} \rangle$.

* $\int dx \cdot \exp(-iax^2/2) = \sqrt{(2\pi/ia)}$; * $\int dx \cdot \exp(ix^2/2a) = \sqrt{(2\pi ia)}$.

$$\sqrt{(2\pi/ia)} = \int dB \cdot \exp(-ia(f/a + B)^2/2) = \int dB \cdot \exp[-i(f^2/2a + Bf + \frac{1}{2}aB^2)]$$

$$= \int df \exp[-i(f^2/2a)] \int dB \cdot \exp[-i(Bf + \frac{1}{2}aB^2)].$$

$$2\pi = \sqrt{(2\pi/ia)} \int df \exp[i(f^2/2a)] = \int df \int dB \cdot \exp[-i(Bf + \frac{1}{2}aB^2)].$$

$$\rightarrow 1 = (2\pi\hbar)^{-1} \int df \int dB \cdot \exp[-i(Bf + \frac{1}{2}\alpha B^2)/i\hbar]. \quad \langle a = \alpha/\hbar; f' = f/\hbar \rangle$$

$$(8) \quad 1 = \Pi_{a,x} \int Df^a \int dB^a \cdot \exp[\int dx^4 (B^a f^a + \frac{1}{2}a B^a B^a)/i\hbar].$$

By employing variable $f^a(\varepsilon^a)$, we are to do integral on the delta function.

(9) Gauss Integral Formula with Grassmann number = $\{\bar{C}^a, C^a\}$

https://en.wikipedia.org/wiki/Grassmann_integral

Grassmann number definition: $\bar{C}^a \cdot C^a + C^a \cdot \bar{C}^a = 0$.

*This is classical number-zation of anti-commutable spinor ψ .

$$\psi * \psi + \psi \cdot \psi = i\hbar \delta(\mathbf{x}' - \mathbf{x}).$$

$$\det \mathbf{A} = \Pi_{a,x} \int D\bar{C}^a \int DC^a \exp[\int dx^4 \cdot \bar{C}^a(x) \mathbf{A} C^a(x)].$$

$$(9) \quad \Delta = \det |ic \partial_\mu \mathbf{D}_\mu| = \Pi_{a,x} \int D\bar{C}^a \int DC^a \exp[\int dx^4 \cdot \chi \bar{C}^a(x) \cdot ic \partial_\mu \mathbf{D}_\mu C^a(x)/i\hbar].$$

(10) Total Quantized Lagrangean of General Gauge Field.

$$\text{I} : R_{CF} \equiv |f\rangle \langle i | \Pi_{a,\mu,\nu,x} \int DA^a_\mu \int D\Pi^a_\nu \cdot \exp[\int dx^4 \langle \mathcal{L}_{CF}(A^a_\mu; \partial_\nu A^a_\mu) / i\hbar \rangle].$$

$$\text{II} : \Delta = \det |ic \partial_\mu \mathbf{D}_\mu| = \Pi_{a,x} \int D\bar{C}^a \int DC^a \exp[\int dx^4 \cdot \chi \bar{C}^a(x) \cdot ic \partial_\mu \mathbf{D}_\mu C^a(x) / i\hbar].$$

$$\text{III} : 1 = \Pi_{a,x} \int D\varepsilon^a \int dB^a \cdot \delta(ic \partial_\mu \mathbf{A}^a_\mu - f^a) \exp[\int dx^4 (B^a f^a + \frac{1}{2}a B^a B^a) / i\hbar] \cdot \Delta.$$

After all, multiplying (III) × (I) is to yield the total Lagrangean.

We do integration on the delta function by $\{D\varepsilon^a\}$.

$$R_{QF} = \Pi_{a,\mu,\nu,x} \int D\varepsilon^a \cdot \int DA^a_\mu \int D\Pi^a_\nu \int DB^a \int D\bar{C}^a \int DC^a \cdot \exp[\int dx^4 \langle \mathcal{L}_{CF} / i\hbar \rangle] \cdot$$

$$\delta(ic \partial_\mu \mathbf{A}^a_\mu - f^a) \cdot \exp[\int dx^4 (B^a f^a + \frac{1}{2}a B^a B^a) / i\hbar] \cdot \exp[\int dx^4 \cdot \chi \bar{C}^a(x) \cdot ic \partial_\mu \mathbf{D}_\mu C^a(x) / i\hbar]$$

$$= \Pi_{a,\mu,\nu,x} \int DA^a_\mu \int D\Pi^a_\nu \int DB^a \int D\bar{C}^a \int DC^a \cdot \exp[\int dx^4 \langle \mathcal{L}_{CF} / i\hbar \rangle]$$

$$\cdot \exp[\int dx^4 (ic \partial_\mu \mathbf{A}^a_\mu B^a + \frac{1}{2}a B^a B^a) / i\hbar] \cdot \exp[\int dx^4 \cdot \chi \bar{C}^a(x) \cdot ic \partial_\mu \mathbf{D}_\mu C^a(x) / i\hbar].$$

$$= \Pi_{a,\mu,\nu,x} \int DA^a_\mu \int D\Pi^a_\nu \int DB^a \int D\bar{C}^a \int DC^a \cdot$$

$$\exp[\int dx^4 \langle \mathcal{L}_{CF} + ic \partial_\mu \mathbf{A}^a_\mu B^a + \frac{1}{2}a B^a B^a + \chi \bar{C}^a(x) \cdot ic \partial_\mu \mathbf{D}_\mu C^a(x) \rangle / i\hbar].$$

$$(10) \quad \mathcal{L}_{QF} = \mathcal{L}_{CF} + ic \partial_\mu \mathbf{A}^a_\mu B^a + \frac{1}{2}a B^a B^a + \chi \bar{C}^a(x) \cdot ic \partial_\mu \mathbf{D}_\mu C^a(x).$$

$$\mathcal{L}_{CF} \equiv -\frac{1}{4} F^a_{\mu\nu} F^a_{\mu\nu} \equiv -\frac{1}{4} (\partial_\mu A^a_\nu - \partial_\nu A^a_\mu - f_b^a c A^b_\mu A^c_\nu)^2.$$